

Cryptographic Hash Functions Part II

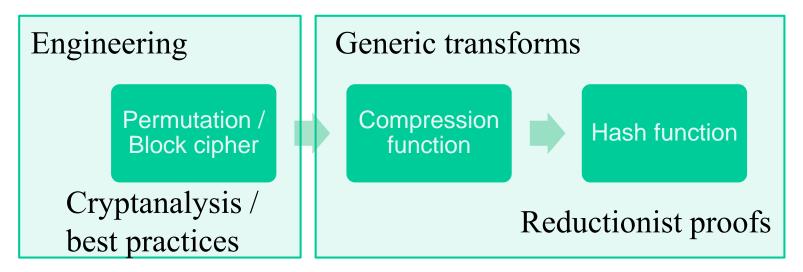
Cryptography 1

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Hash function design

- Create fixed input size building block
- Use building block to build compression function
- Use "mode" for length extension





(LENGTH-EXTENSION) MODES



Merkle-Damgård construction

Given:

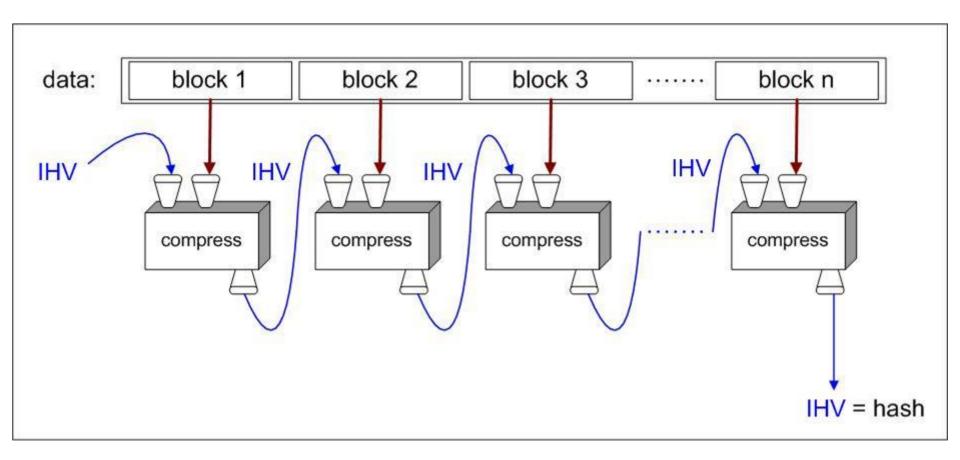
• compression function: $CF : \{0,1\}^n \ge \{0,1\}^n \to \{0,1\}^n$

Goal:

• Hash function: $H : \{0,1\}^* \to \{0,1\}^n$



Merkle-Damgård - iterated compression





Merkle-Damgård construction

- assume that message *m* can be split up into blocks
 *m*₁, ..., *m*_s of equal block length *r*
 - most popular block length is r = 512
- compression function: $CF : \{0,1\}^n \ge \{0,1\}^n \rightarrow \{0,1\}^n$
- *intermediate hash values* (length *n*) as *CF* input *and* output
- message blocks as second input of CF
- start with fixed initial *IHV*₀ (a.k.a. *IV* = *initialization vector*)
- iterate CF: $IHV_1 = CF(IHV_0, m_1)$, $IHV_2 = CF(IHV_1, m_2)$, ..., $IHV_s = CF(IHV_{s-1}, m_s)$,
- take $h(m) = IHV_s$ as hash value
- advantages:
 - this design makes *streaming* possible
 - hash function analysis becomes compression function analysis
 - analysis easier because domain of *CF* is finite



padding

- padding: add dummy bits to satisfy block length requirement
- non-ambiguous padding: add one 1-bit and as many
 0-bits as necessary to fill the final block
 - when original message length is a multiple of the block length, apply padding anyway, adding an extra dummy block
 - any other non-ambiguous padding will work as well



Merkle-Damgård strengthening

- let padding leave final 64 bits open
- encode in those 64 bits the original message length
 - that's why messages of length ≥ 2⁶⁴ are not supported
- reasons:
 - needed in the proof of the Merkle-Damgård theorem
 - prevents some attacks such as
 - trivial collisions for random IV

 $- \text{ now } h(IHV_0, m_1 || m_2) = h(IHV_1, m_2)$

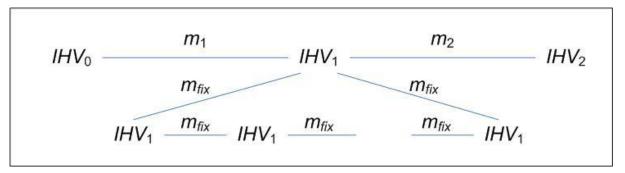
see next slide for more



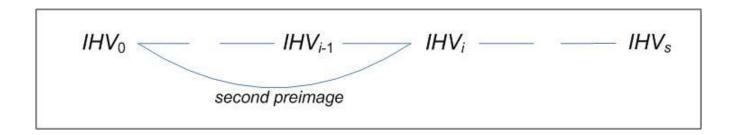
Merkle-Damgård strengthening, cont'd

fixpoint attack

fixpoint: *IHV*, *m* such that *CF*(*IHV*,*m*) = *IHV*



long message attack





compression function collisions

- collision for a compression function: m_1 , m_2 , *IHV* such that $CF(IHV, m_1) = CF(IHV, m_2)$
- pseudo-collision for a compression function: m_1 , m_2 , IHV_1 , IHV_2 such that $CF(IHV_1, m_1) = CF(IHV_2, m_2)$
- Theorem (Merkle-Damgård): If the compression function CF is pseudo-collision resistant, then a hash function h derived by Merkle-Damgård iterated compression is collision resistant.
 - Proof: Suppose $h(m_1) = h(m_2)$, then
 - If m_1 and m_2 same size: locate the iteration where the collision occurs
 - Else a pseudo collision for CF appears in the last blocks (cont. length)
- Note:
 - a method to find pseudo-collisions does not lead to a method to find collisions for the hash function
 - a method to find collisions for the compression function is almost a method to find collisions for the hash function, we 'only' have a wrong *IHV*



Sponges

Given:

• *permutation*: $f : \{0,1\}^b \to \{0,1\}^b$

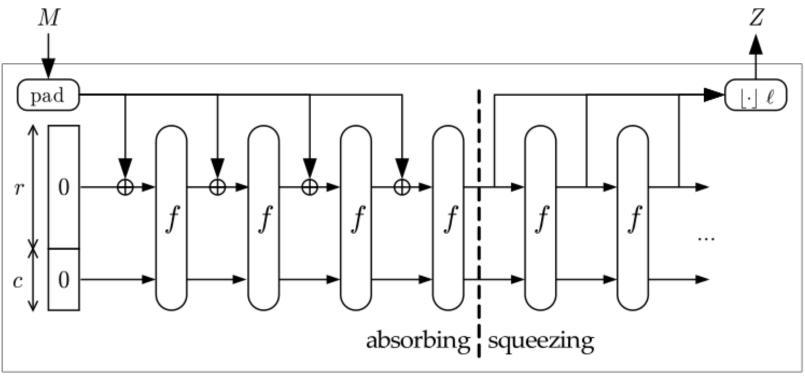
Goal:

- Hash function: H: {0,1}* → {0,1}ⁿ
 (actually H: {0,1}* → {0,1}*)
- (Already includes CF design, more later)



Sponges

- Used and introduced in SHA3 aka Keccak
 - Guido Bertoni, Joan Daemen, Michaël Peeters and Gilles Van Assche



sponge



Intercourse: Random oracles

- Models the perfect hash function
- Truely random function without any structure
- Best attacks: Generic attacks (No structure available!)

Issue:

• No way to build a RO with polynomial description

Mind Model:

- Lazy-sampling
 - Imagine a black box implementing the function
 - For every new query, a random response is sampled
 - For old queries, former response is used



Sponge security

• Theorem (Indifferentiability from a random oracle): If f is a random permutation, the expected complexity for differentiating a sponge from a random oracle is $\sqrt{\pi} 2^{c/2}$.

- Note:
 - Neat way to simplify security arguments
 - Implies bounds for all attacks that use less than $\sqrt{\pi} 2^{c/2}$ queries
 - Bounds are those of generic attacks against a random oracle

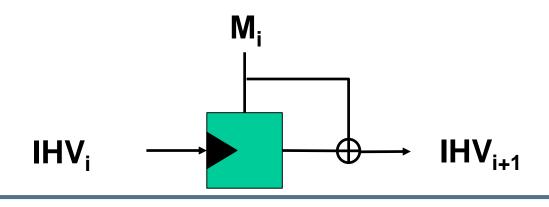


COMPRESSION FUNCTION DESIGN



Block-Cipher-based designs

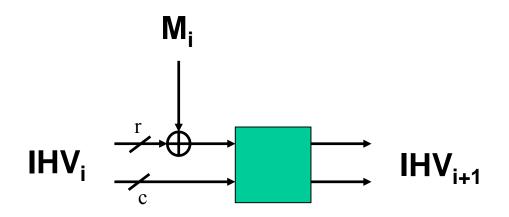
- Traditional approach
- Many possible modes
 - see Preneel, Govaerts, Vandewalle. Hash functions based on block ciphers: a synthetic approach. CRYPTO'93
 - security: Black, Rogaway, Shrimpton. Black-Box Analysis of the Block-Cipher-Based Hash-Function Constructions from PGV. CRYPTO'02
- Most popular: Matyas-Meyer-Oseas





Permutation-based designs

- Less frequent use
- Keccak compression function:



Important: NEVER hand out bits last c bits of IHV!



Security

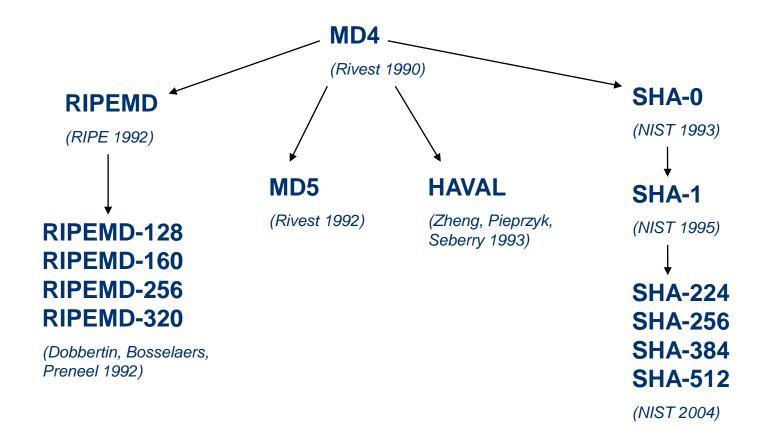
- Generally analyzed in idealized models:
 - "Black-box models"
 - Ideal cipher model
 - Random oracle model
 - Random permutation model
- Proofs assuming underlying building block behaves like such an idealized building block



BASIC BUILDING BLOCKS



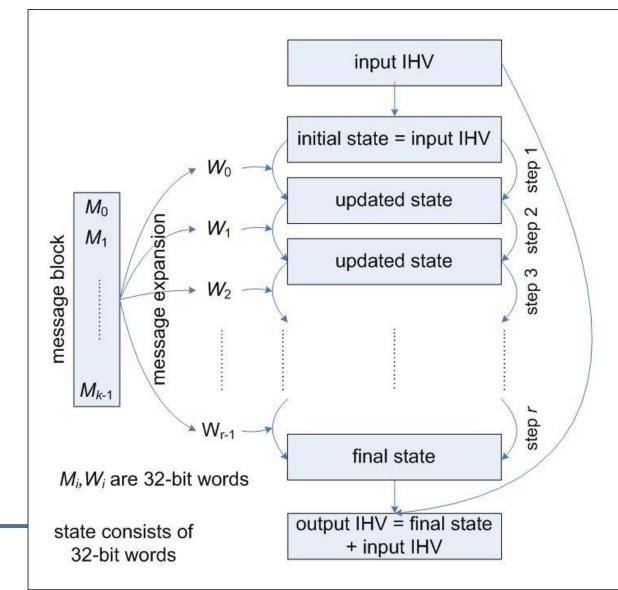
the MD4 family of hash functions





design of MD4 family compression functions

message block split into words message expansion input words for each step $HV \rightarrow$ initial state each step updates state with an input word final state 'added' to IHV (feed-forward)





design details

- MD4, MD5, SHA-0, SHA-1 details:
 - 512-bit message block split into 16 32-bit words
 - state consists of 4 (MD4, MD5) or 5 (SHA-0, SHA-1) 32-bit words
 - MD4: 3 rounds of 16 steps each, so 48 steps, 48 input words
 - MD5: 4 rounds of 16 steps each, so 64 steps, 64 input words
 - SHA-0, SHA-1: 4 rounds of 20 steps each, so 80 steps, 80 input words
 - message expansion and step operations use only very easy to implement operations:
 - bitwise Boolean operations
 - bit shifts and bit rotations
 - addition modulo 2³²
 - proper mixing believed to be cryptographically strong

message expansion

• MD4, MD5 use *roundwise permutation*, for MD5:

$$- W_0 = M_0, W_1 = M_1, \dots, W_{15} = M_{15},$$

- $W_{16} = M_1, W_{17} = M_6, ..., W_{31} = M_{12}$, (jump 5 mod 16)
- $W_{32} = M_5$, $W_{33} = M_8$, ..., $W_{47} = M_2$, (jump 3 mod 16)
- $W_{48} = M_0, W_{49} = M_7, ..., W_{63} = M_9 \text{ (jump 7 mod 16)}$
- SHA-0, SHA-1 use recursivity

e

- $W_0 = M_0, W_1 = M_1, ..., W_{15} = M_{15},$
- SHA-0: $W_i = W_{i-3}$ XOR W_{i-8} XOR W_{i-14} XOR W_{i-16} for i = 16, ..., 79
- problem: *k*th bit influenced only by *k*th bits of preceding words, so not much diffusion
- SHA-1: $W_i = (W_{i-3} \text{ XOR } W_{i-8} \text{ XOR } W_{i-14} \text{ XOR } W_{i-16}) <<<1$ (additional rotation by 1 bit,

this is the only difference between SHA-0 and SHA-1)



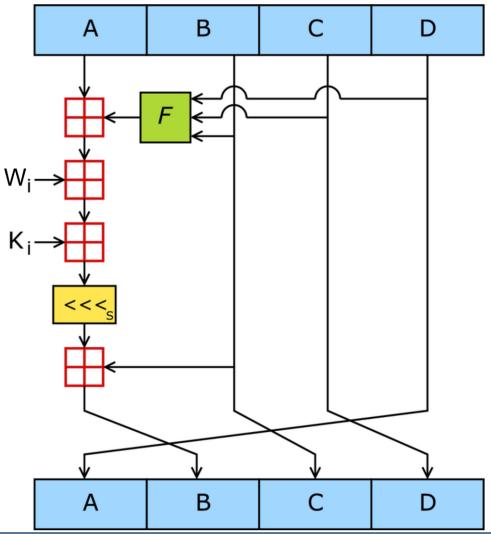
Example: step operations in MD5

- in each step only one state word is updated
- the other state words are rotated by 1
- state update:

 $A' = B + ((A + f_i(B, C, D) + W_i + K_i) <<< s_i)$ K_i, s_i step dependent constants, + is addition mod 2^{32} , f_i round dependend boolean functions: $f_i(x, y, z) = xy OR(\neg x)z$ for i = 1, ..., 16, $f_i(x,y,z) = xz \ OR \ y(\neg z) \ for \ i = 17, ..., 32,$ $f_i(x,y,z) = x XOR y XOR z$ for i = 33, ..., 48, $f_i(x,y,z) = y XOR(y OR(\neg z))$ for i = 49, ..., 64,these functions are nonlinear, balanced, and have an avalanche effect



step operations in MD5





provable hash functions

- people don't like that one can't prove much about hash functions
- reduction to established 'hard problem' such as factoring is seen as an advantage
- Example: VSH Very Smooth Hash
 - Contini-Lenstra-Steinfeld 2006
 - collision resistance provable under assumption that a problem directly related to factoring is hard
 - but still far from ideal
 - bad performance compared to SHA-256
 - all kinds of multiplicative relations between hash values exist
 - not post-quantum secure



Life cycles of popular cryptographic hashes (the "Breakout" chart)																							
Function	1990	1991	1992	1993	1994	1995	1996	1997	1998	1999	2000	2001	2002	2003	2004	2005	2006	2007	2008	2009	2010	2011	2012
Snefru																							
MD4																							
MD5																							
MD2																							
RIPEMD																							
HAVAL-128																							
SHA-0																							
SHA-1																							
RIPEMD-128 [1]																							
RIPEMD-160																							
SHA-2 family																		[2]					
SHA-3																							
(Keccak)																							
Key Unbroken Weakened Broken Deprecated																							
[1] Note that 128-bit hashes are at best 2^64 complexity to break; using a 128-bit hash is irresponsible based on sheer digest length.																							
[2] In 2007, the	[2] In 2007, the NIST launched the SHA-3 competition because "Although there is no specific reason to believe that a practical attack on any of the SHA-2 family of																						

[2] In 2007, the <u>NIST launched the SHA-3 competition</u> because "Although there is no specific reason to believe that a practical attack on any of the SHA-2 family of hash functions is imminent, a successful collision attack on an algorithm in the SHA-2 family could have catastrophic effects for digital signatures." One year later the first strength reduction was published.

The Hash Function Lounge has an excellent list of references for most of the dates. Wikipedia now has references to the rest.



Real life attacks on MD5

Example Hash-then-Sign in Browser

🏈 Inloggen Rabo Internetbankieren – Rabobank - W	Vindows Internet Ex	xplorer		
G 🕞 🗢 🗟 https://bankieren.rabobank.nl/kl	anten/	👻 🔒 Rabobank Nederland [NL]	🗟 🍫 🗙 🛃 Google	<mark>ب</mark> ۵
🚖 Favorites 🛛 🖶 🔻 🚺 Outlook - hooghsja@h	n 🏾 🌈 http://wv	× Website Identification		n ▼ Page ▼ Safety ▼ Tools ▼ 🔞 ▼ ≫
Certificate	loggen n	VeriSign has identified this site as: Rabobank Nederland Utrecht, Utrecht		
General Details Certification Path		NL This connection to the server is encrypted.		
Show: <ali></ali>	alleen in me	Should I trust this site?	Rabobank	Aanvragen
Field Value	de S-toets n	View certificates	UW PIN	Heeft u geen toegang tot Rabo Internetbankieren?
Serial number 43.03.02 c8 5-28 d8 bc 9a 82 Signature algorithm sha1RSA Signature hash algorithm sha1 Valid from veriSign Class 3 Extended Vali Valid to vrijdag 19 juli 2012 2:00:00 Valid to vrijdag 19 juli 2013 1:59:59 Subject bankieren.rabobank.nl, Name Pithir kev PS& (7048 Rite) CN = bankieren.rabobank.nl OU = Name IT bx O = Rabobank Nederland STREET = Croeselaan 18 E L = Utrecht S = Utrecht S = Utrecht SERIALNUMBER = 30046259	ruk op I (Inlog bets uw pincod de toegangscod	as in de Random Reader		Met Rabo Internetbankieren kunt u altijd via Internet uw rekeningen inzien en transacties uitvoeren. > Informatie over Rabo Internetbankieren > Bekijk de demo Help > Waarom kan ik niet inloggen ? > Waarom krijg ik de melding (942)? > Waarom krijg ik de melding (947)?
Edit Properties Copy to File Learn more about certificate details		als de adresregel begint met https://bankieren.ra u de veiligheid van uw verbinding? veiligheid	abobank.nl/	
, Done		in 🕰	ternet I Protected Mode: Or	n 🕼 🔻 🖲 100% 👻



Wang's attack on MD5

- two-block collision
 - for any input *IHV*, identical for the two messages i.e. $IHV_0 = IHV_0'$, $\Delta IHV_0 = 0$
 - *near-collision* after first block: $IHV_1 = CF(IHV_0, m_1), IHV_1' = CF(IHV_0, m_1'),$ with ΔIHV_1 having only a few carefully chosen ±1s
 - full collision after second block: $IHV_2 = CF(IHV_1, m_2), = CF(IHV_1', m_2'),$ i.e. $IHV_2 = IHV_2', \Delta IHV_2 = 0$
- with *IHV*₀ the standard *IV* for MD5, and a third block for padding and MD-strengthening, this gives a collision for the full MD5



chosen-prefix collisions

- latest development on MD5
- Marc Stevens (TU/e MSc student) 2006
 - paper by Marc Stevens, Arjen Lenstra and Benne de Weger, EuroCrypt 2007
- Marc Stevens (CWI PhD student) 2009
 - paper by Marc Stevens, Alex Sotirov, Jacob Appelbaum, David Molnar, Dag Arne Osvik, Arjen Lenstra and Benne de Weger, Crypto 2007
 - rogue CA attack



MD5: identical IV attacks

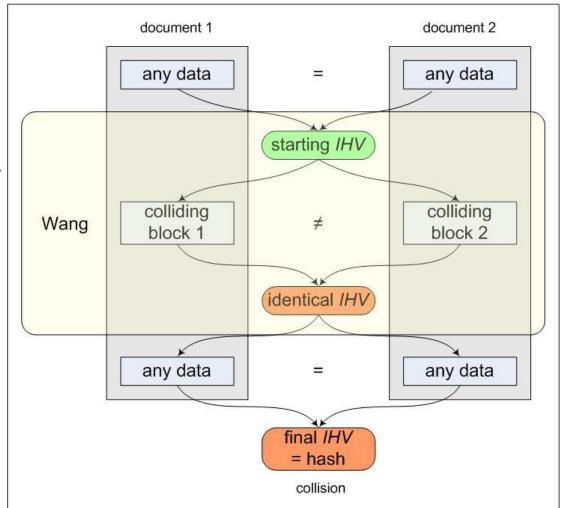
- all attacks following Wang's method, up to recently
- MD5 collision attacks work for any starting *IHV*

data before and after the collision can be *chosen at will*

 but starting *IHV*s must be identical

data before and after the collision *must be identical*

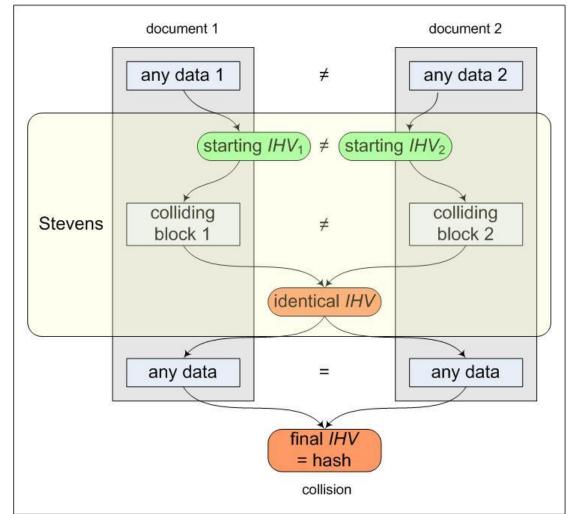
called random collision





MD5: different IV attacks

- new attack
 - Marc Stevens, TU/e
 - Oct. 2006
- MD5 collisions for any starting pair {*IHV*₁, *IHV*₂}
 - data before the collision needs not to be identical data before the collision can still be chosen at will, for each of the two documents data after the collision still must be identical
- called chosen-prefix collision





indeed that was not the end in 2008 the ethical hackers came by

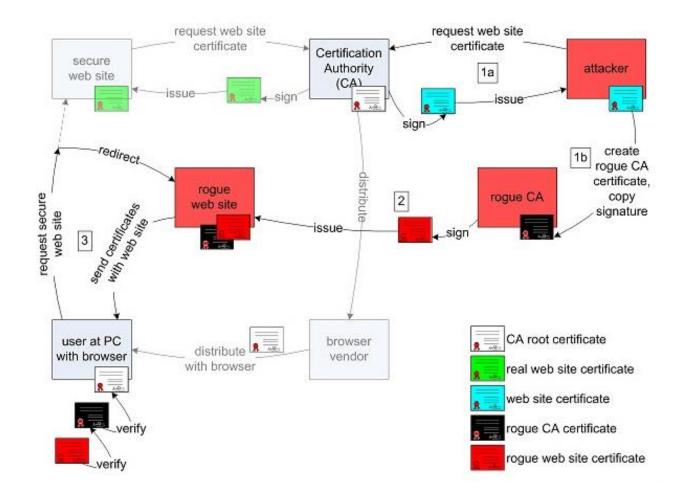
observation: commercial certification authorities still use MD5

idea: proof of concept of realistic attack as wake up call \rightarrow attack a real, commercial certification authority

purchase a web certificate for a valid web domain but with a "little tweak" built in prepare a rogue CA certificate with identical MD5 hash the commercial CA's signature also holds for the rogue CA certificate



Outline of the RogueCA Attack





legitimate website certificate		rogue CA certificate					
serial number		serial number					
commercial CA name		commercial CA name					
validity period		validity period					
	chosen prefixes	rogue CA name					
domain name		1024 bit RSA public key					
Gomain name		v3 extensions					
		Subject = CA					
2048 bit RSA public key	collision bits	tumor					
v3 extensions	identical suffixes						
Subject = End Entity							
signature		signature					



problems to be solved

predict the serial number predict the time interval of validity at the same time a few days before more complicated certificate structure "Subject Type" after the public key small space for the collision blocks is possible but much more computations needed not much time to do computations to keep probability of prediction success reasonable



how difficult is predicting?

time interval:

CA uses automated certification procedure certificate issued exactly 6 seconds after click

I Approve

I Do Not Approve

serial number :

Nov	3	07:4	44:08	2008	GMT	643006
Nov	3	07:4	45:02	2008	GMT	643007
Nov	3	07:4	46:02	2008	GMT	643008
Nov	3	07:4	47:03	2008	GMT	643009
Nov	3	07:4	48:02	2008	GMT	643010
Nov	3	07:4	49:02	2008	GMT	643011
Nov	3	07:	50:02	2008	GMT	643012
Nov	3	07:	51:12	2008	GMT	643013
Nov	3	07:	51:29	2008	GMT	643014
Nov	3	07:	52:02	2008	GMT	have a guess



the attack at work

estimated: 800-1000 certificates issued in a weekend procedure:

- 1. buy certificate on Friday, serial number S-1000
- 2. predict serial number S for time T Sunday evening
- 3. make collision for serial number S and time T: 2 days time
- 4. short before *T* buy additional certificates until S-1
- 5. buy certificate on time *T*-6 hope that nobody comes in between and steals our serial number *S*



to let it work

cluster of >200 PlayStation3 game consoles (1 PS3 = 40 PC's)

complexity: 2⁵⁰ memory: 30 GB

 \rightarrow collision in 1 day





result

success after 4th attempt (4th weekend)

purchased a few hundred certificates (promotion action: 20 for one price) total cost: < US\$ 1000



conclusion on MD5

- at this moment, 'meaningful' hash collisions are
 - easy to make
 - but also easy to detect
 - still hard to abuse realistically
- with chosen-prefix collisions we come close to realistic attacks
- to do *real* harm, second pre-image attack needed
 - real harm is e.g. forging digital signatures
 - this is not possible yet, not even with MD5
- More information: http://www.win.tue.nl/hashclash/



Questions?



proof of birthday paradox

• probability that all k elements are distinct is

$$\prod_{i=0}^{k-1} \frac{t-i}{t} = \prod_{i=0}^{k-1} \left(1 - \frac{i}{t}\right) \le \prod_{i=0}^{k-1} e^{-\frac{i}{t}} = e^{-\sum_{i=0}^{k-1} \frac{i}{t}} = e^{-\frac{k(k-1)}{2t}}$$

and this is $< \frac{1}{2}$ when $k(k-1) > (2 \log 2)t$ ($\approx k^2$) ($\approx 1.4 t$)